

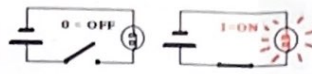


Massachusetts Institute of Technology (MIT)



Lecture by Pr. Bob Gallagher

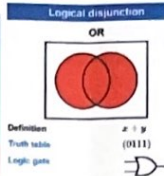
Boole (1815-1864) & Shannon (1916-2001)



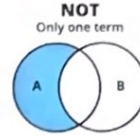
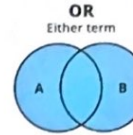
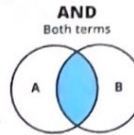
Logical addition (disjunction)

A	B	F=A ∨ B
0	0	0
0	1	1
1	0	1
1	1	1

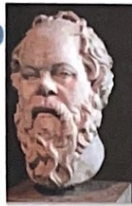
A	B	A ∨ B
True	True	True
True	False	True
False	True	True
False	False	False



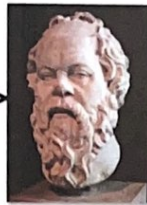
BOOLEAN LOGIC



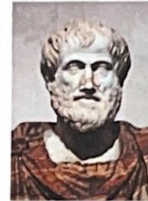
Good logic



Socrates was a philosopher



philosophers are men



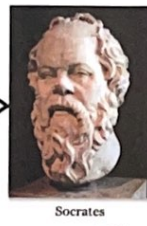
Socrates was a man



Bad logic



Socrates was a man



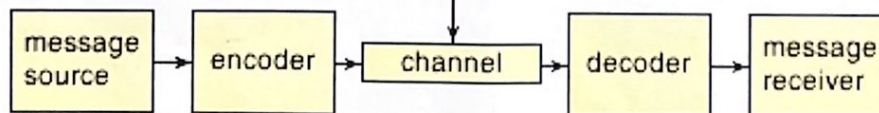
philosophers are men



Socrates was a philosopher



noise



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To save inf. we should keep it in 3 places:

- HDD 1 90% ok 10% fail
- site 1 90% ..
- www 1 90% ..

$1 - 0.1 \cdot 0.1 \cdot 0.1 = 0.999$ probability to save information 99.9%

Walking in Oxford on a cold and rainy day

DEPARTMENT OF STATISTICS

With prof. Matthias Winkel



80% chance of rain
says the Met Office in its weather forecast for Oxford.

CHALK + TALK



ink + think



Good way 1. listening 2. first way of processing 3. writing

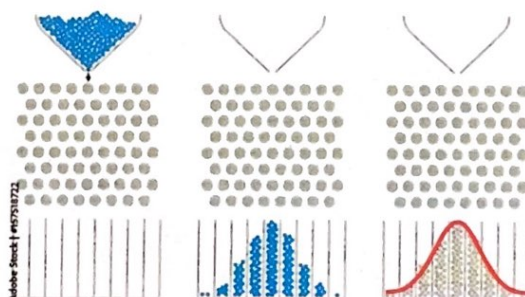
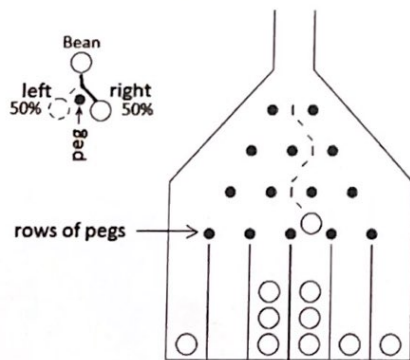


Markoff Chain Probability Model

for Oxford Weather



If it is Rainy today => there is an 80% chance that it will be rainy tomorrow.



School $\rightarrow$ gravity $\rightarrow$ Motion == formalism ==> University $E = MC^2$ $\Phi = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$

Motivation: 80% chance of rain
Let A_j be the event of rain at Jam on day j of this term, $1 \leq j \leq n$
Suppose the events A_j each have probability p , independently

Oxford				
Tue 13th	Wed 14th	Thu 15th	Fri 16th	
10° 9°	13° 10°	13° 8°	11° 7°	
70%	70%	70%	100%	

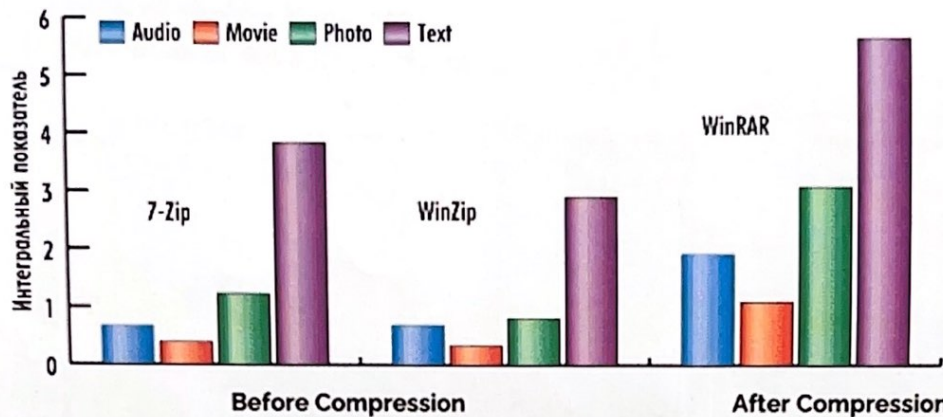
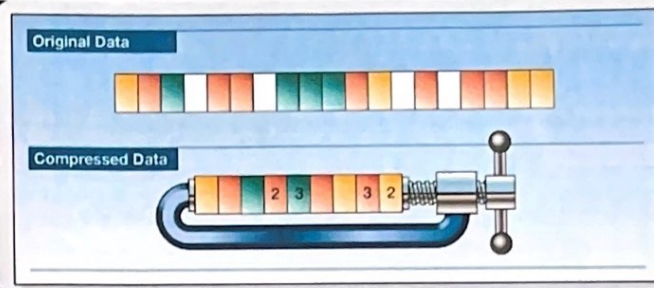


then take notes on the lecture yourself

Motivation: 80% chance of rain

Let A_j be event of rain at gam⁴⁰
on day j of this term, $1 \leq j \leq n$ ³⁹

Comparison of the compression ratio of popular archivers



Before Compression			After Compression	
Data	Symbol	Frequency	Symbol	Bit Code
AAAAAAABCCCCCDDDEEEEE ↓	A	7	A	00
	B	1	B	111
	C	6	C	01
	D	2	D	110
	E	5	E	10

Entropy
compression ratio

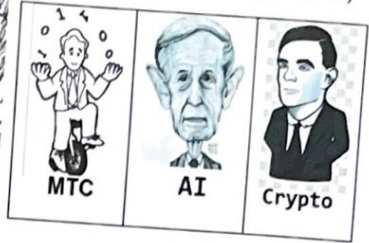
Before Compression = $21 \times 8 \text{ bits} = 198 \text{ bits}$
 After Compression = $7 \times 2 \text{ bits} + 1 \times 3 \text{ bits} + 6 \times 2 \text{ bits} + 2 \times 3 \text{ bits} + 5 \times 2 \text{ bits} = 45 \text{ bits}$

+0.4 to Exam
 +0.2 to Exam
 $\lg(32) = 5.17$
 $36 = 5.2$
 +

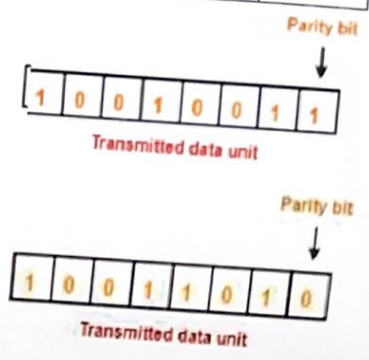
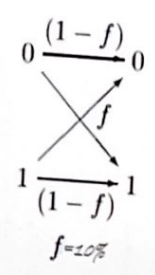
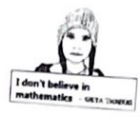




Sir Dr. D. MacKay,
University of Cambridge
(22 April 1967 – 14 April 2016)



"I believe in clean energy,
but I also believe in mathematics"



S ENCODER t CHANNEL f = 10% r DECODER ŝ

Source sequence s	Transmitted sequence t
0	000
1	111

The repetition code R₃

source message s 0 0 1 0 1 1 0

t 000 000 111 000 111 111 000

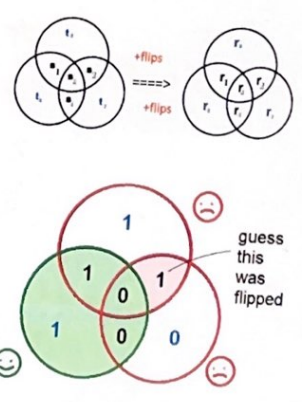
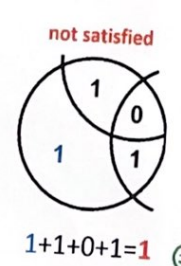
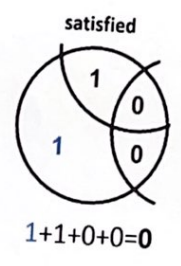
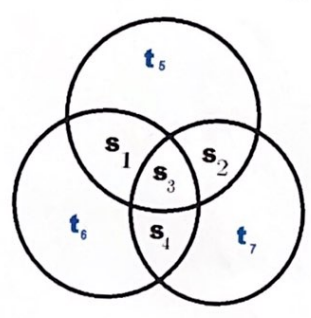
n 000 001 000 000 101 000 000

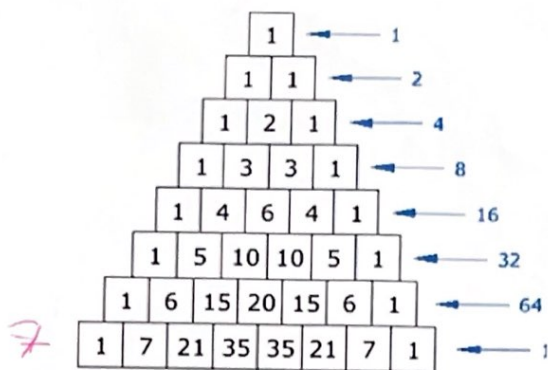
r 000 001 111 000 010 111 000

corrected errors *

undetected errors *

7.4. Hamming code. $\frac{4}{\Sigma} \rightarrow \frac{7}{t}$





7
8 1 8 28
9 9 36

Shannon Hartley Theorem

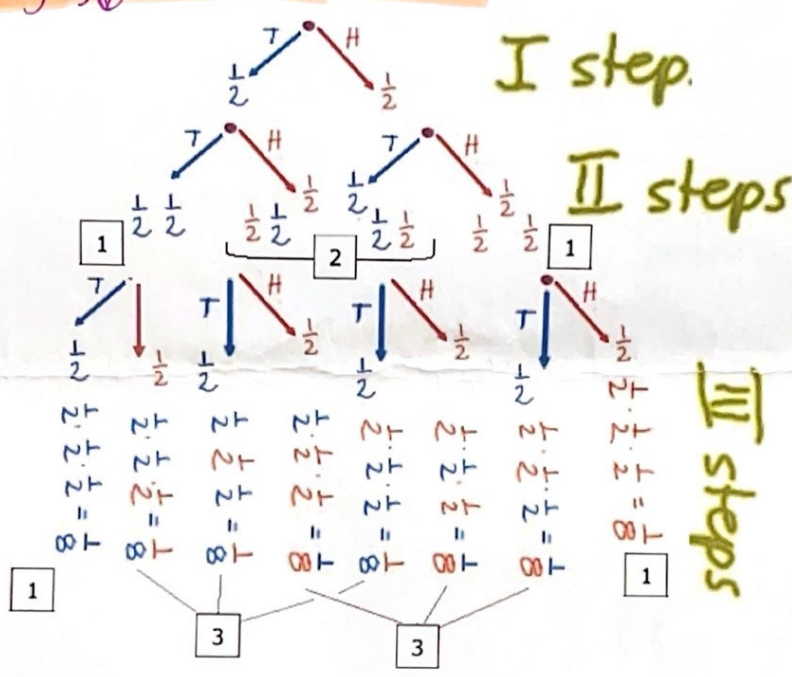
This is a measure of the *capacity* on a channel; it is impossible to transmit information at a faster rate without error.

$$C = B \log_2(1 + S/N)$$

- C = capacity (in bit/s)
- B = bandwidth of channel
- S = signal power (in W)
- N = noise power (in W)

It is more usual to use SNR (in dB) instead of power ratio (as with terrestrial and commercial communications systems: $S/N \gg 1$, then rewriting in terms of $\log_{10}$.

$$C = B \frac{\log_{10}(S/N)}{\log_{10} 2} = B \frac{10 \log_{10}(S/N)}{10 \cdot \log_{10} 2} = B \frac{SNR}{3.01}$$



$$\begin{aligned} (a+b)^0 &= 1 \\ (a+b)^1 &= a+b \\ (a+b)^2 &= a^2 + 2ab + b^2 \\ (a+b)^3 &= a^3 + 3a^2b + 3ab^2 + b^3 \\ (a+b)^4 &= a^4 + 4a^3b + 6a^2b^2 + 4ab^3 + b^4 \\ (a+b)^5 &= a^5 + 5a^4b + 10a^3b^2 + 10a^2b^3 + 5ab^4 + b^5 \end{aligned}$$



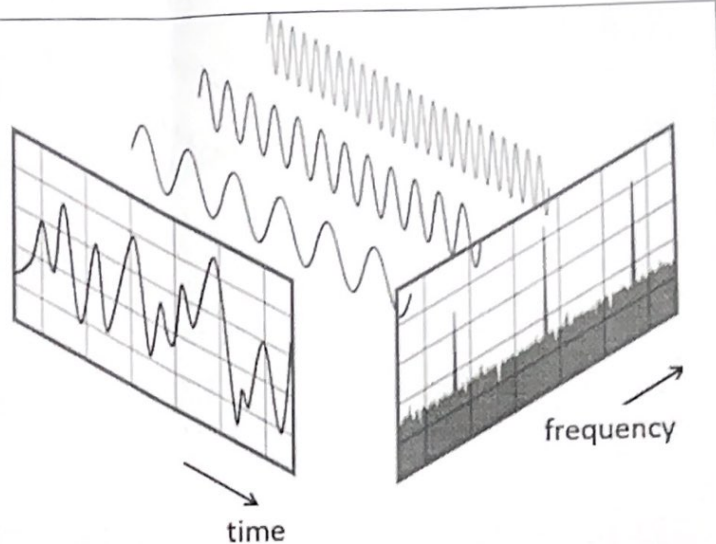
$K=2$ ordering of $\begin{matrix} m_1 & m_2 \\ a & a \\ b & b \end{matrix}$ is $\frac{n!}{m_1! \cdot m_2!} = \frac{n!}{m_1! \cdot (n-m_1)!} = \frac{n!}{m_2! \cdot (n-m_2)!}$

$$(1+x)^4 = 1 + 4x + 6x^2 + 4x^3 + x^4$$

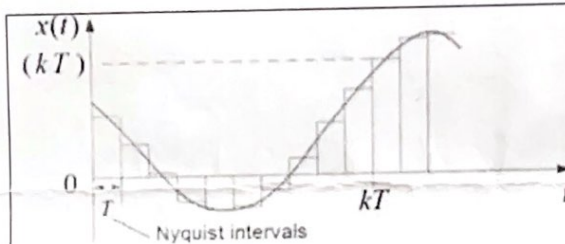
$$(y+x)^9 = y^9 + 9xy^8 + 36x^2y^7 + 84x^3y^6 + 126x^4y^5 + 126x^4y^5 + 84x^5y^4 + 36x^6y^3 + 9x^7y^2 + x^9$$

+0.2 to Exam

Fourier transform

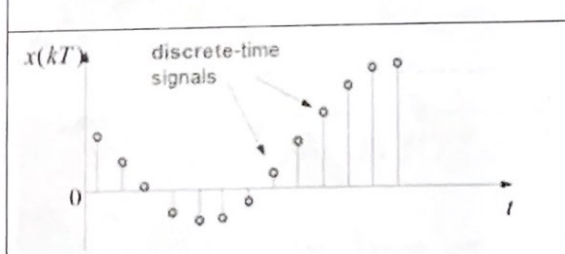
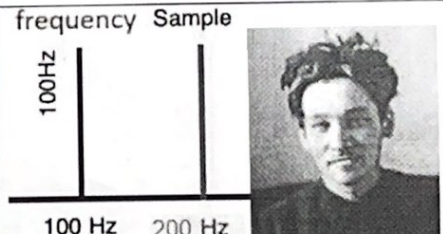
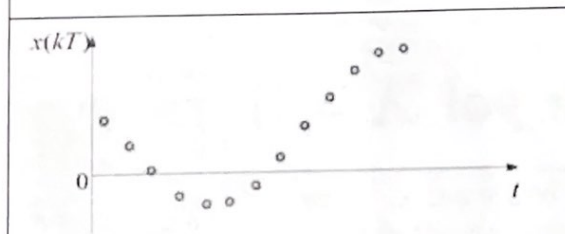
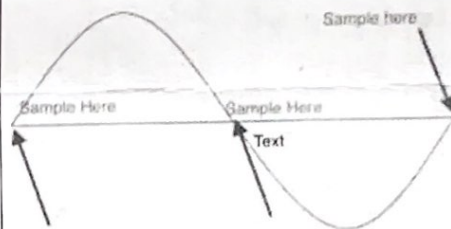


Sampling. Kotelnikov-Nyquist Theorem



Time intervals T , through which readings $s(kT)$ are taken, are called Nyquist intervals.

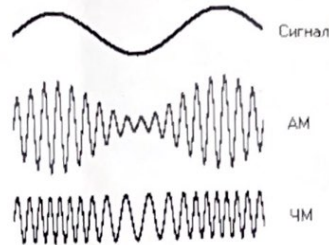
Sine with period T Sampling at $T/2$



$$F_{\text{sample}} \geq 2 * F_{\text{max}}$$

$$(T_{\text{sample}} \leq T_{\text{min}}/2)$$

$s = 5 \sin(2\pi \cdot 9t) + 3 \sin(2\pi \cdot 8t)$ $F_{\text{sample}}?$ 5 amplitude
 the highest frequency component is 9Hz, thus 2.8 33
 $F_{\text{sample}} \geq 2 \cdot 9 = 18 \text{ Hz}$ 52
 -0.2 to Exam



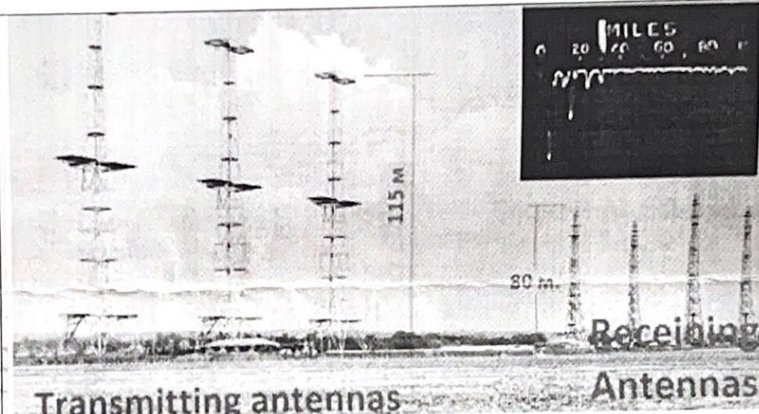
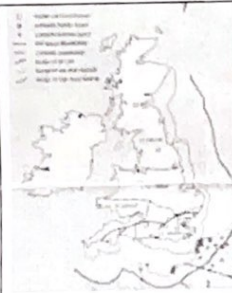
Reginald A. Fessenden

(October 6, 1866 – July 22, 1932)

first transmission of speech by radio (1900), and the first two-way radiotelegraphic communication across the Atlantic Ocean (1906)

"No organization engaged in any specific field of work, ever invents any important development in that field, or adopts any important development in that field, until forced to do so by outside competition." Oxford University Press. The Quarterly Journal of Economics, Feb., 1926, p. 262.

Battle of Britain (3 month 3 weeks) 10.07-31.10.1940



Transmitting antennas
Receiving Antennas
Radar played a major role in the Battle of England

H. Nyquist



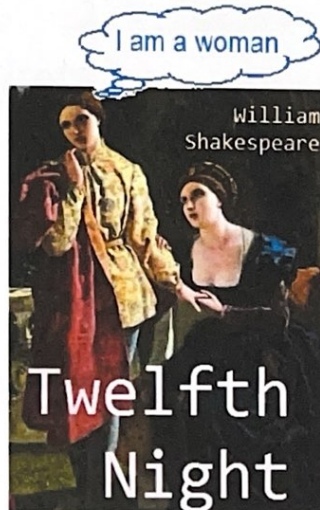
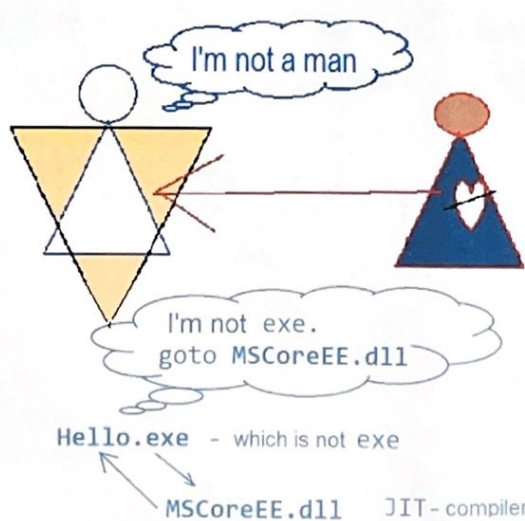
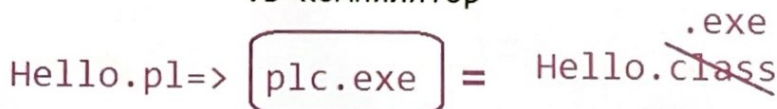
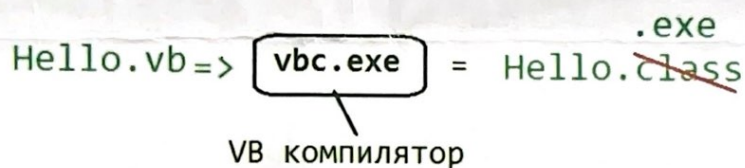
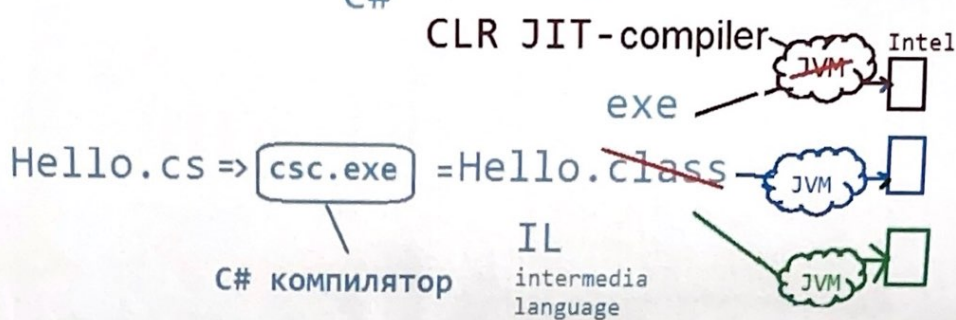
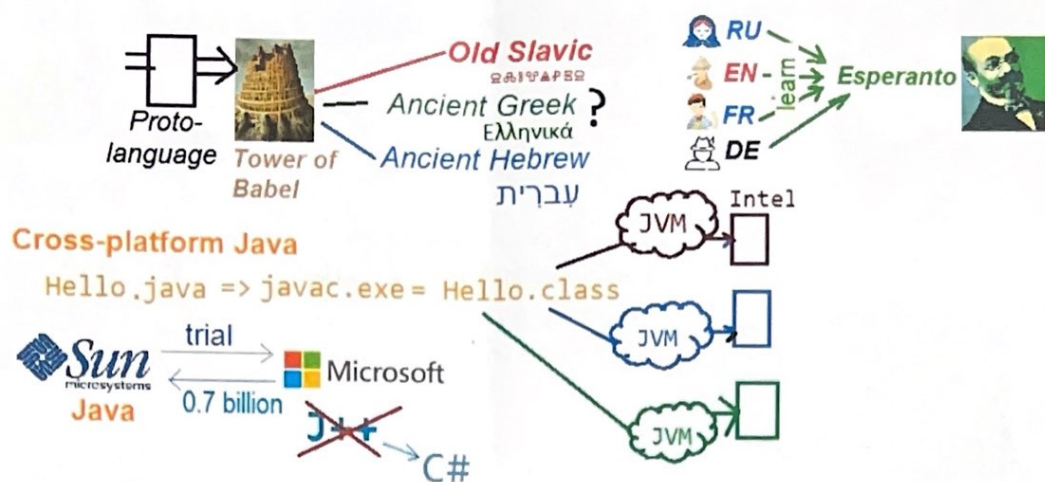
$$W = K \log m$$

Where W is the speed of transmission of intelligence,
 m is the number of current values,
and, K is a constant.



$$H = n \log s$$

$$= \log s^n.$$

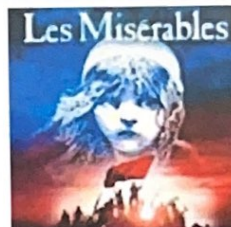


É. Galois (1811-1832) Les Misérables | Do You Hear the People Sing?



Example

There are $6!$ ways to order the letters of GALOIS
If randomly reorder the letters what is probability that the Vowels (A, O, I) are all before consonants (G, L, S)?



aoi gls $3! = 6$
 aoi pls
 aoi gsl
 aoi spl
 aoi slp
 aoi lps
 aoi lsp } 6 i $1 \cdot 3! = 6$

A revolution may well put end to despotism, but it never produce true reform in way of thinking.

aoi gls 3 letters $3!$
 iao gsl
 ...
 1st position
 i o pls $2 \cdot 3!$
 a i o pls $3! \cdot 3!$

i $1 \cdot 3!$ $1 \cdot 6$
 oi $2 \cdot 3!$ $2 \cdot 6$
 aoi $3! \cdot 3!$ $3 \cdot 6$
 $P_{rc} = \frac{3! \cdot 2!}{5!}$

I. Kant

ABBA $\frac{4!}{2! \cdot 2!}$ The number of arrangements of the N objects.

$\underbrace{x_1, \dots, x_1}_{m_1}$ $\underbrace{x_2, \dots, x_2}_{m_2}, \dots, \underbrace{x_k, \dots, x_k}_{m_k}$ where $n = m_1 + m_2 + \dots + m_k$

$$\frac{n!}{m_1! m_2! \dots m_k!}$$



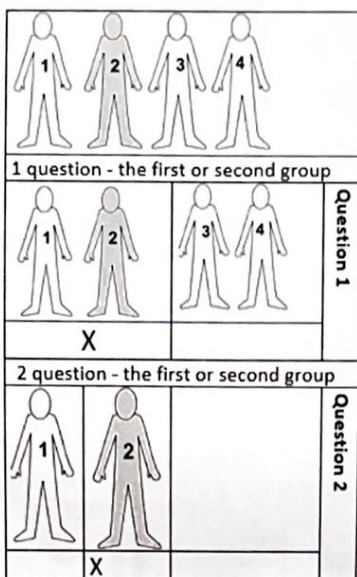
Say **NO** to the **first**



Say **YES** to the **second** if it is better than the first



Say **NO** to the **third** only if it is worse than all the others



Average number of questions =
 $2 \cdot 0.25 + 2 \cdot 0.25 + 2 \cdot 0.25 + 2 \cdot 0.25 = 2$

Average number of questions =

$1 \cdot 0.5 +$	$2 \cdot 0.25 +$	$3 \cdot 0.125 +$	$3 \cdot 0.125$

Question 1. Is this Zuckerberg?	50%	$1 \cdot 0.5$
Question 2. Is this Sergey Brin?	25%	$2 \cdot 0.25$
Question 3. Is this Stefan from BMW?	12.5%	$3 \cdot 0.125$
So Prince Saud	12.5%	$3 \cdot 0.125$
Average number of questions =		1.75

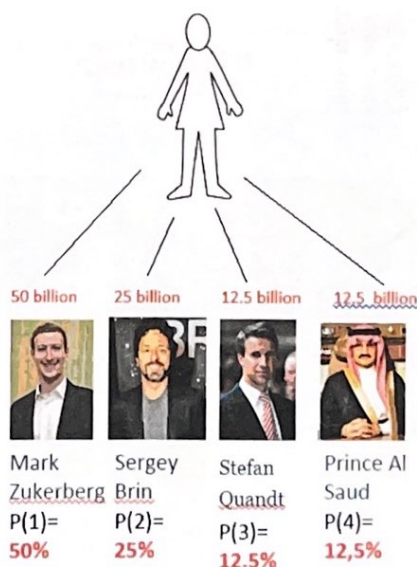
Quantifying information

$$S(x) = \sum_{i=1}^n p(i) \log_2 \frac{1}{p(i)}$$

Quantifying information

$$I(x_i) = \log_2 \left(\frac{1}{p_i} \right)$$

number of bits required to encode choice



$\log_2(26) = 4.8$
 or 4.7
 + 0.25 to Exam

What should you do at home:
Register free hosting on

- ✓ freeasphosting.net
At home because many hosting services do not register from one IP address.

ASP.NET
Hosting .NET 7

FREE ASP.NET Hosting
FREE Domain Hosting
FREE MS SQL Database
INCLUDES .NET Core
Full Trust Permissions

SIGN UP FOR FREE

Create Your Free Site

✉ Confucius@studentweb.cc

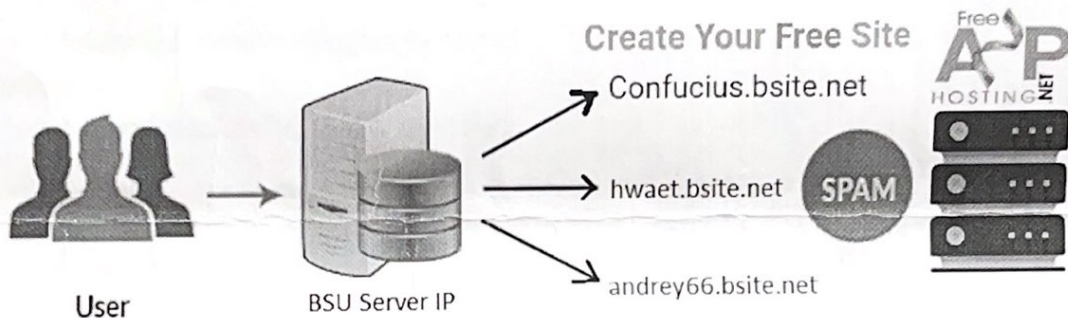
👤 https://Confucius.bsite.net

🔒

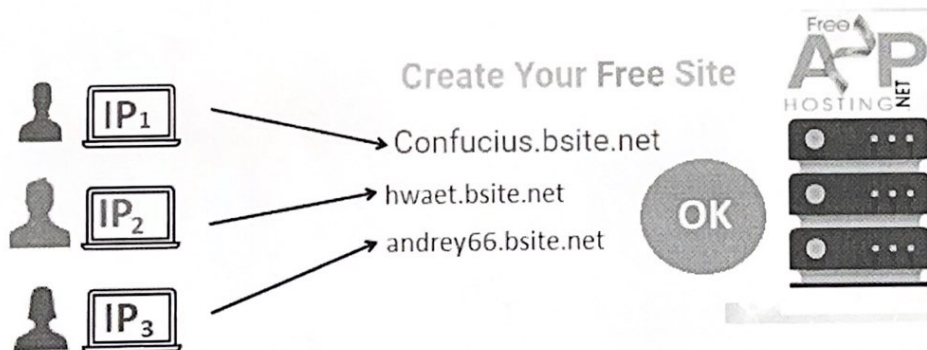
By signing up with our service you agree to our [Terms & Conditions](#).

Create Site

If several dozen hosting attempts to register from one IP address, the freeasphosting.net server may decide that this is a SPAMer and block it.



And if registration is carried out from different computers (with different IP addresses), then the freeasphosting.net server does not raise any suspicions.



After you have registered on the server, send me your address (which you received during registration) by email.

What should you do in class:

0. Come up with a good name for your site.

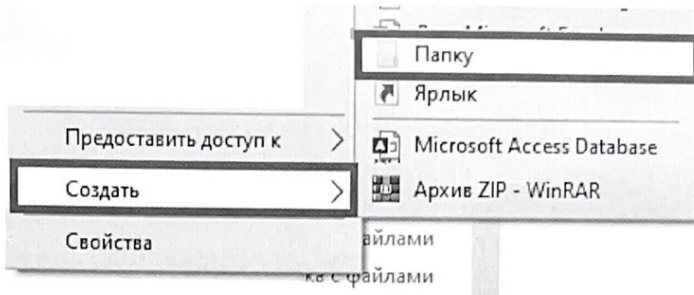
I came up with a name for my site - Confucius (in my opinion, this is a good name)
www.confucius.bsite.net

1. On a disk or on a flash drive, make a folder that matches the name of the site

www.confucius.bsite.net

Новый том (D:) >

www.confucius.bsite.net



2. In a folder **D:\www.confucius.bsite.net** create a folder for Projects

D:\www.confucius.bsite.net\Projects

3. In a folder **D:\www.confucius.bsite.net\Projects** create a folder for Projects Number 0

D:\www.confucius.bsite.net\Projects\0

4. In a folder **D:\www.confucius.bsite.net\Projects\0** create file *index.htm*

10.179.32.238
 20ра 10ра 200

index.html



3.1.1

40.2 to Exam

